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Time Replacement Optimization Models for Urban Transportation Buses with Indexation to Fleet Reserve

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Abstract – An efficient management of physical assets in general and the urban transportation buses in particular, has as objective the optimization of its Life Cycle Cost (LCC), being the optimization of its maintenance and the determination of the right moment of its withdrawal or its renewal, essential elements for optimization of the capital investments.

These aspects are related to the determination of the optimal dimension of the fleet reserve, aiming the maximization of its availability and the investment minimization. This can be reached through several algorithms that ought to be in consideration aspects like the maintenance costs, reseller cost, and inflation, among others.

This is reached through the adequate maintenance policies, being these scheduled and or on-condition predictive or any kind of planned ones. This type of decisions are determinant to maximize the LCC and, by consequence, the dimension of reserve fleet.

It is through this perspective that the identification of the right moment of replacement or total renewal of an asset can be a strategic element in the competitiveness of the organizations by reducing the costs that can come from there.

The validation of the management models to be implemented will be done in the road transports sector of passengers' transportation and the models and the results have the potential to help this strategic sector in the global economy.

Keyword: *Equipment Removal; LCC; Fleet reserve; On-Condition Maintenance; Scheduled Maintenance; Predictive Maintenance.*

I. INTRODUCTION

The present article refers the replacement of buses, with indexation to the fleet reserve in companies of urban transportation buses.

In the present globalized economy, the companies' survival or, in a more generalized way, of the organizations depends on its ability to innovate. For that, they endlessly search new tools that may contribute for its continuous improvement.

The maintenance management or physical assets corresponds to a fundamental side for that goal. To guarantee the maximum availability of the equipment is a main goal of any maintenance section and this fact is determinant so that the companies are able to respond to the competitive challenges in which they are involved. A maintenance program that focus on

the assets' management will only be successful if it stops to have an error management routine to the management of the life cycle of the assets.

The passenger transportation buses' management is an essential activity for the guarantee of the optimal compliance of its life cycle, which implies the combination of actions of management, technical and economical, in the sense of obtaining higher availability at rational costs, [1-5].

The cost of an asset's life cycle corresponds to the sum of all the spent capitals on the support of that asset since its conception and manufacturing, going through the operation until the end of its useful life [2]. It is understood that the useful lifetime goes until the deactivation of the equipment and that this could be different from the effective lifetime of the item, like it is the case of the equipment with fast technologic obsolescence.

The LCC of an asset can be significantly superior to the value of the initial investment and, in many cases, it's defined right on the project phase. [3]

The analysis of the cost of the life cycle it's a foreseeing and, therefore generally different methods are used in cost estimate, [7] and others like the Activity-Based Costing (ABC) [8]. The simulation method of Monte Carlo is another tool to deal with uncertainty.

To support the analysis of the cost of the life cycle there are rules as the referred in [9-10]. The rule about the assets management [11] is a good source of guidelines to the assets management that can be applied to any sector.

Though, the systematized study in this area remains underdeveloped, having the need of applying and creating new models of equipment management that can bring more benefits to the companies, in order to improve its productivity and quality of service, having in consideration the side of the environmental sustainability, including the rules of quality management, environment, safety, maintenance and energy [12], although it is known that many companies maintain equipment in function, even when its operation is no longer viable because they do not accompany its economic cycle, which has exogenous implications, in the case of passengers transportation, in the size of the fleet reserve.

According to [14], the traditional production systems are built over the scale economy principle. This author even

illustrates a problem of equipment replacement, in a Lean Thinking context. [15] Says that the technological transformation as the motivation for replacement of the equipment. In scientific references is commonly assumed that technology continuously develops according to a well-defined function.

[16] Shows that combining continuous and discrete time models, the time to replace equipment is lower when the technology applied is superior.

According to [17], "the assessment of an profit is established by future benefits expected by cash flows referred to the present value by a discount rate that reflects the risk of the decision." Consequently, methods that consider the time value of money are the most suitable.

According to [18], the method of Equivalent Uniform Annual Cost CAUE is appropriate in the analysis of the company's operational activities, with investments that may repeat. Furthermore, the standardization of investment results equivalent to annual values makes the analysis of these results will easy the decision making. The use of this method is to determine what is the year with the lowest equivalent annual cost, which indicates the best time to replace the technical active [19].

The calculation of the equivalent annual cost is due to the use of the Capital Recovery Factor and it is through it that we can compare two or more investment opportunities and determining which ideal replacement of equipment time, taking into account information such as: value of the investment or acquisition; resale value or residual value at the end of each year; operating costs and cost of capital or minimum attractive rate [19].

The problem of determining the economic life of equipment for the purpose of replacing could be identified in four types of situation [20]:

1. When the good is already inadequate for the activity;
2. When the good has reached its limit of life;
3. When the good is already obsolete due to technological advances;
4. When more efficient methods show to be more economic.

In a certain point in the life cycle of a profit it is important to assess if keep it running or replaced. For this purpose, you must satisfy the following [12]:

- i. Availability of new technologies;
- ii. Fulfillment of safety standards or other mandatory;
- iii. Availability of spare parts;
- iv. Obsolescence that may limit its use.

After the listed aspects of the last point of the life cycle of the equipment, it is important to characterize some calculation methods for determining the appropriate time to replace it. For this purpose it is necessary to take into account several variables:

- acquisition value
- Value of expiration
- operating costs

- Maintenance costs
- Operating Costs

- Inflation rate
- Capitalization rate

The majority of previous values of the variables are obtained by history, with the exception of the value expiration. In this case, to get the market value for each particular equipment, that can be not easy for many goods. An alternative it can simulate several types of devaluation such as the following [21]:

- Linear method of depreciation - the decline of the value of the equipment is constant over the years.
- Method of the sum of digits - the annual depreciation is not linear.
- Exponential method - The annual depreciation charge is decreasing over the life of the equipment.

Another method commonly used is the "lifetime" that defines that ends when the maintenance costs exceed the costs of maintenance plus the amortization of the capital of equivalent new equipment. According to [12] there are several methods for determining the economic cycle equipment replacement. The most common are:

- Method of Uniform Annual Rent (MUAR);
- Method of Minimizing Total Average Cost (MCMT);
- MCMT method with the reduction of the present value (MCMT-PVR);

In [22], illustrates the effective use of fixed assets as a major objective in the management of companies in the urban passenger transport sector.

Companies in the urban transport sector, the efficient use of profits is linked to a well-structured policy assessment and fleet replacement. Some cases of fleet replacement applied to the city bus segment are reported in [22-25].

The adoption of a single decision criteria is restrictive, given that costs, efficiency and level of service should be evaluated simultaneously. Methods such as Multi Attribute Utility Theory (MAUT), Analytical Hierarchy Process (AHP) and Quality Function Deployment (Quality Function Deployment - QFD) have been used to accommodate multiple decision makers and multiple decision criteria. However, were not found in the literature approaches consolidated using these methods in the replacement of public transport vehicles. It is also referred the use of stochastic models in conjunction with neural networks to model the creation of a replacement vehicle.

[26] Presents a proposal of a generic stochastic process model based on neural networks called Stochastic Neural Process (NSP) that can be applied in problems involving stochastic phenomena or periodic behavior and characteristics. Through neuronal networks of the PEN models the behavior of the time series of these phenomena without requiring a priori information about the series, by generating synthetic time series equally adaptable to the historical series. Some cases of using neural networks and stochastic models are reported in the literature [27-33].

II. BUSES REPLACEMENT MODELS

The replacement of equipment is an umbrella concept that embraces selection of similar profits, but new ones, to replace the existing ones, to evaluate the profits that act in ways completely different performance of the same function. This is the case of obsolete buses may be replaced by new models that operate in a similar manner.

Replacement decisions are critical for the company, because they are generally irreversible, ie, have no cash and require large amounts of money.

There are several reasons to make economic action to do the replacement of equipment. The deterioration is one of the causes, and is manifested by excessive operating costs and by the increasing of the maintenance costs. There are situations here the replacement of a standard operation conduce to the loss of the device ability to operate efficiently, ie, it becomes inappropriate.

Importa fazer a caracterização de métodos de cálculo adequados para determinação da altura adequada à substituição dos autocarros de transporte urbano de passageiros. Para o efeito, é necessário ter em consideração diversas variáveis:

So it is important perform a characterization of the appropriate methods of calculation for determining the proper time of replacement of buses for urban passenger transport. Indeed it is necessary to take in account several variables:

- Cost of acquisition (CA)
- Value of expiration (VC)
- The operating costs (EC)
 - Maintenance costs (CM)
 - Operating costs (CO)
- inflation rate (θ)
- capitalization rate (i)

The majority of previous values of the variables are obtained by history, with the exception of the value expiration. In this case, to get the market value for each particular equipment, that can be not easy for many goods. As an alternative it can simulate several types of devaluation such as the following: [21]

- Linear depreciation method– that lies on the assumption that the decline of the value of the equipment is constant over the years.
- Method of the sum of the digits - the annual depreciation is not linear.
- The Exponential method - The annual depreciation charge is decreasing over the life of the equipment.

A. Linear Depreciation Method

This method assumes that the decrease in the value of the device is constant over the years and is calculated by the following formula:

$$d_j = \frac{CA - VC_n}{N} \quad (1)$$

d_j Annual depreciation quota
 CA Acquisition cost of equipment

VC_n Residual value of the equipment at the end of N periods
 N Lifetime corresponds to
 j $j=1,2,3 \dots n$
 V_n Value of the equipment over a period $n = 1, 2, 3 \dots n$.

The value of the equipment V_n , in a period n lower N is given by:

$$V_j = CA - j * d \quad (2)$$

B. Method of Sum of Digits

In this method, the annual depreciation is not linear and is calculated the following way:

$$d_j = 2 * \frac{N - (j - 1)}{N + 1} * \frac{CA - VC_n}{N} \quad (3)$$

$$V_n = CA - d_j \quad (4)$$

C. Exponential Method

The exponential method emphasizes an annual depreciation that decreases over the life of the equipment. The calculation formula is as follows:

$$d_j = VC_{j-1} * (1 - \sqrt[N]{\frac{VC_n}{CA}}) \quad (5)$$

$$V_n = CA - d_j \quad (4)$$

According to [12] the equipment can be replaced by various criteria. The financial aspect, a usual criterion is the "economic cycle" which determines the optimal period which minimizes the average total costs of operation, maintenance and capital immobilization.

Another method commonly used is the "lifetime" that defines that the equipment ends when their maintenance costs exceed the costs of maintenance plus the amortization of the capital of equivalent new equipment.

However, despite being possible from the depreciation values of market power pass to the analysis of equipment replacement, should be taken into account two other variables, which are:

- The capitalization rate, called for i
- The inflation rate, called by θ

These rates are related as follows:

$$i_A = i + i * \theta$$

According to [12] there are several methods for determining the economic cycle equipment replacement. The most common are:

- Method of Uniform Annual Income (MRAU)
- Method of Minimizing Total Average Cost (MCMT)

- MCMT method with the reduction of the present value (MCMT-PVR)

This article will use the Uniform Method of Annual Income (MRAU), this makes use of the following data:

- Acquisition cost of equipment
- expiration values (calculated according to the methods exposed ago)
- Maintenance Costs and Exploration over the years
- Apparent rate

D. Net present value in year n (VPL_n)

$$VPL_n = CA + \sum_{j=0}^n \frac{CM_j + CO_j}{(1+i_A)^j} - \frac{V_n}{(1+i_A)^j} \quad (6)$$

With,

CA Acquisition cost of equipment

CM_j Maintenance costs in year $j = 1, 2, 3 \dots n$

CO_j Operating costs in year $j = 1, 2, 3 \dots n$

i_A Apparent rate

V_n Value of the equipment over a period $n = 1, 2, 3 \dots n$.

E. Uniform Annual Rent (RAU_n)

$$RAU_n = \frac{i_A(1+i_A)^j}{(1+i_A)^j - 1} * (CA + \sum_{j=0}^n \frac{CM_j + CO_j}{(1+i_A)^j} - \frac{V_n}{(1+i_A)^j}) \quad (7)$$

$$RAU_n = \frac{i_A(1+i_A)^j}{(1+i_A)^j - 1} * VPL_n \quad (8)$$

With,

VPL_n Net present value $n = 1, 2, 3 \dots n$

The minor RAU calculated value indicates the respective period (multi-year), in which the equipment must be replaced. This value is equivalent to a minimum income that the equipment would cost annually.

The MCMT determines the lowest average cost of ownership of the equipment and the respective it occurs that corresponds to the optimal time of replacement. They are not considered capital costs and the rate of inflation. The calculation procedure is as follows:

$$C'_n = \frac{\sum_{j=0}^n CM_j + CO_j}{n} \quad C''_n = \frac{CA - V_n}{n} \quad C_n = C'_n + C''_n \quad (9)$$

With,

n Number of years $n = 1, 2, 3 \dots n$

C_n Average total cost

The MCMT - RVP the calculation procedure is identical to the previous one, with the exception that are considered capital costs and the inflation rate. The various values of maintenance and disposal, over the years, are reduced to present value, according to the following procedure:

$$C'_n = \frac{1}{n} \sum_{j=1}^n \frac{CM_j + CO_j}{(1+i_A)^j} \quad C''_n = \frac{CA - \frac{V_n}{(1+i_A)^j}}{n} \quad C_n = C'_n + C''_n \quad (10)$$

III. APPLICATION OF THE MODEL IN THE TRANSPORT SECTOR

The demonstrational application of the equipment replacement model will be made then in the road transport sector, with an emphasis on passenger, which corresponds to a strategic sector of the national and global economy. Application of the Model in the Transport Sector

The aim of this paper to present a model replacement bus passenger transport leading to the rationalization of the reserve fleet in a global perspective, to create integrated models that allow:

- Optimizing the management of their lifecycle;
- Optimizing the time of replacement;
- Optimizing the fleet reserve.

To develop this study and the fulfillment of the objectives listed in the previous paragraph, should be taken into consideration variables related aspects such as the technological aspects, the duly itemized direct operating costs, downtime costs, as well as indicators economic applicable, such as inflation and interest rates, among others.

In the first phase of the data collection operation for preparation of LCC is made, a road transport company. Based on these data is initiated the development of simulation models from a small number of buses, taken as a pilot to validate the replacement model.

A. Characterization of buses

In this phase the variables relevant to the purpose have been defined such as: Operation, maintenance, service user and the environment. Further characterize aspects that significantly affect the operating performance of the buses (existence and type of air-conditioning, engine power, etc.).

In the preparation of the models the following variables were used: the year of manufacture of the buses; starting year of operation; trademark; model; type of vehicle; maintenance costs; cost of operation; etc.

10 cars divided into two brands and five different models of buses, as shown in Table 1 were selected.

Nº FROTA	MARCA	MODELO	TIPO	ANO FABRICO	ANO INICIO OPERAÇÃO	USAR	TIPO MOTION	COMBUSTIVEL	POTÊNCIA	LOTAGEM	CUSTO DE AQUISIÇÃO
X1	Marca A	Mod A	STANDARD	1993	1994	19	EURO 1	GASÓLEO	157 KW	96	110 658,31 €
X2	Marca A	Mod A	STANDARD	1993	1994	19	EURO 1	GASÓLEO	157 KW	96	110 658,31 €
X3	Marca A	Mod A	STANDARD	1993	1994	19	EURO 1	GASÓLEO	157 KW	96	110 658,31 €
Y1	Marca B	Mod B	STANDARD	1996	1997	16	EURO 2	GASÓLEO	245 HP	84	120 459,69 €
Y2	Marca B	Mod C	STANDARD	1998	1999	14	EURO 2	GASÓLEO	245 HP	87	130 005,68 €
XX1	Marca A	Mod D	STANDARD	2002	2003	10	EURO 3	GASÓLEO	205 KW / 275 CV	95	164 453,66 €
XX2	Marca A	Mod D	STANDARD	2002	2003	10	EURO 3	GASÓLEO	205 KW / 275 CV	95	164 453,66 €
XX3	Marca A	Mod D	STANDARD	2002	2003	10	EURO 3	GASÓLEO	205 KW / 275 CV	95	164 453,66 €
YY1	Marca B	Mod E	STANDARD	2004	2005	8	EURO 3	GASÓLEO	202 KW / 275 HP	90	159 515,57 €
YY2	Marca B	Mod E	STANDARD	2004	2005	8	EURO 3	GASÓLEO	202 KW / 275 HP	90	159 515,57 €

Fig. 1. Table Characteristics of Buses

B. Background data of Buses

At this stage, the focus corresponds to the identification and collection of primary data that are the basis for the analysis. The data should be relevant to the description of fleet costs and related activities, and should support the understanding of strategic economic and business information. Should be given priority to the information concerning procedures of operation, maintenance and planning. In this context, the historical data

for each vehicle target of the study were collected, as can be seen below in Tables 2-6.

MP	PROTA	MARCA	MODELO	TPO	1993/2004	1993/2005	1993/2006	1993/2007	1993/2008	1993/2009	1993/2010	1993/2011	1993/2012
X1	Marca A	Mod A	STANDARD	64.350	60.330	57.723	55.942	56.345	49.740	43.303	43.925	52.995	
X2	Marca A	Mod A	STANDARD	65.115	56.358	56.834	51.397	49.177	46.204	51.157	51.717	51.285	
X3	Marca A	Mod A	STANDARD	59.443	61.238	54.267	48.957	57.007	44.875	48.723	53.096	49.445	
Y1	Marca B	Mod B	STANDARD	76.259	66.421	62.647	62.666	66.841	60.873	59.402	68.865	71.815	
Y2	Marca B	Mod C	STANDARD	53.133	62.303	57.642	54.533	59.587	54.370	53.635	58.966	62.455	
X01	Marca C	Mod C	STANDARD	51.644	54.267	51.732	53.327	57.290	59.664	51.308	56.715	51.502	
X02	Marca A	Mod C	STANDARD	53.276	52.633	50.789	51.587	55.364	59.941	54.007	58.395	47.335	
X03	Marca C	Mod D	STANDARD	55.174	61.196	65.235	67.506	69.173	65.586	63.213	59.034	59.707	
Y11	Marca B	Mod E	STANDARD	45.241	62.290	59.294	45.639	43.728	39.754	37.387	36.907	33.382	
Y12	Marca B	Mod E	STANDARD	41.407	60.632	58.460	42.029	41.095	35.199	36.405	32.364	35.807	

Fig. 2. Table Kms / year traveled by bus

MP	PROTA	MARCA	MODELO	TPO	1993/2004	1993/2005	1993/2006	1993/2007	1993/2008	1993/2009	1993/2010	1993/2011	1993/2012
X1	Marca A	Mod A	STANDARD	30264.90	28363.93	27.130.49	25966.42	26481.91	23381.02	20554.19	20544.52	24884.14	
X2	Marca A	Mod A	STANDARD	30617.19	26476.37	26734.20	24157.16	23111.62	21775.97	24042.82	24308.38	24102.71	
X3	Marca A	Mod A	STANDARD	27960.50	27677.71	25607.27	23011.81	26793.50	21907.89	22896.16	24644.45	23235.53	
Y1	Marca B	Mod B	STANDARD	36287.52	31942.05	30107.66	31058.06	34924.41	31651.68	30880.30	36850.56	37244.90	
Y2	Marca B	Mod C	STANDARD	30279.80	34036.58	32979.69	30308.99	32339.88	29930.74	29642.79	30260.56	33708.88	
X01	Marca A	Mod D	STANDARD	26573.88	26521.47	26030.07	30514.56	32382.50	33170.70	29524.83	32271.03	29954.20	
X02	Marca A	Mod D	STANDARD	26142.80	26092.65	27777.00	30000.99	31285.99	32287.05	29208.09	31261.21	28799.38	
X03	Marca A	Mod D	STANDARD	23805.20	27541.08	29257.93	30362.90	31133.31	32510.44	31603.41	29250.89	29959.95	
Y11	Marca B	Mod E	STANDARD	27841.84	30468.07	34056.07	29820.73	25206.95	23787.89	23202.57	22349.87	21015.75	
Y12	Marca B	Mod E	STANDARD	20272.53	35945.74	34059.89	29566.56	24957.10	23541.97	23002.29	22780.90	22872.63	

Fig. 3. Table of Litres of Fuel consumed / year by bus

MP	PROTA	MARCA	MODELO	TPO	1993/2004	1993/2005	1993/2006	1993/2007	1993/2008	1993/2009	1993/2010	1993/2011	1993/2012
X1	Marca A	Mod A	STANDARD	3.905.616	5.971.008	5.134.074	5.397.205	6.064.174	7.050.356	10.061.222	8.059.976	6.377.635	
X2	Marca A	Mod A	STANDARD	5.517.326	5.316.204	5.066.544	5.703.937	14.500.477	7.273.456	6.115.872	5.342.126	4.126.685	
X3	Marca A	Mod A	STANDARD	4.996.606	5.770.214	7.374.537	5.719.627	6.075.232	10.834.244	3.977.556	3.205.322	4.870.615	
Y1	Marca B	Mod B	STANDARD	7.115.054	5.316.635	4.832.605	7.094.322	6.801.935	7.108.364	12.328.564	8.211.222	7.269.778	
Y2	Marca B	Mod C	STANDARD	10.500.798	6.426.156	6.223.432	11.646.116	11.646.116	8.788.896	10.446.752	8.516.626	8.516.626	
X01	Marca A	Mod D	STANDARD	5.446.476	6.426.156	6.223.432	11.646.116	11.646.116	8.788.896	10.446.752	8.516.626	8.516.626	
X02	Marca A	Mod D	STANDARD	3.338.124	6.426.156	6.223.432	11.646.116	11.646.116	8.788.896	10.446.752	8.516.626	8.516.626	
X03	Marca A	Mod D	STANDARD	3.656.506	6.426.156	6.223.432	11.646.116	11.646.116	8.788.896	10.446.752	8.516.626	8.516.626	
Y11	Marca B	Mod E	STANDARD	1.251.516	1.541.935	2.727.556	4.715.516	4.768.544	3.233.054	3.457.635	7.153.104	10.595.444	
Y12	Marca B	Mod E	STANDARD	267.809	1.707.109	2.232.444	4.950.466	6.310.399	6.077.598	6.421.544	5.990.626	6.359.976	

Fig. 4. Table of Operating Costs

MP	PROTA	MARCA	MODELO	TPO	1993/2004	1993/2005	1993/2006	1993/2007	1993/2008	1993/2009	1993/2010	1993/2011	1993/2012
X1	Marca A	Mod A	STANDARD	3.905.616	5.971.008	5.134.074	5.397.205	6.064.174	7.050.356	10.061.222	8.059.976	6.377.635	
X2	Marca A	Mod A	STANDARD	5.517.326	5.316.204	5.066.544	5.703.937	14.500.477	7.273.456	6.115.872	5.342.126	4.126.685	
X3	Marca A	Mod A	STANDARD	4.996.606	5.770.214	7.374.537	5.719.627	6.075.232	10.834.244	3.977.556	3.205.322	4.870.615	
Y1	Marca B	Mod B	STANDARD	7.115.054	5.316.635	4.832.605	7.094.322	6.801.935	7.108.364	12.328.564	8.211.222	7.269.778	
Y2	Marca B	Mod C	STANDARD	10.500.798	6.426.156	6.223.432	11.646.116	11.646.116	8.788.896	10.446.752	8.516.626	8.516.626	
X01	Marca A	Mod D	STANDARD	5.446.476	6.426.156	6.223.432	11.646.116	11.646.116	8.788.896	10.446.752	8.516.626	8.516.626	
X02	Marca A	Mod D	STANDARD	3.338.124	6.426.156	6.223.432	11.646.116	11.646.116	8.788.896	10.446.752	8.516.626	8.516.626	
X03	Marca A	Mod D	STANDARD	3.656.506	6.426.156	6.223.432	11.646.116	11.646.116	8.788.896	10.446.752	8.516.626	8.516.626	
Y11	Marca B	Mod E	STANDARD	1.251.516	1.541.935	2.727.556	4.715.516	4.768.544	3.233.054	3.457.635	7.153.104	10.595.444	
Y12	Marca B	Mod E	STANDARD	267.809	1.707.109	2.232.444	4.950.466	6.310.399	6.077.598	6.421.544	5.990.626	6.359.976	

Fig. 5. Table of Maintenance Costs

MP	PROTA	MARCA	MODELO	TPO	Intervalos periódicos de Revisão (horas)	Programação de Revisões	Intervalos periódicos de Lubrificação (horas)	Programação de Lubrificações
X1	Marca A	Mod A	STANDARD	30.000	A1 A2 A1 A3 A1 A2	25.000	L2 L1 L2 L1 L2	
X2	Marca A	Mod A	STANDARD	30.000	A1 A2 A1 A3 A1 A2	25.000	L2 L1 L2 L1 L2	
X3	Marca A	Mod A	STANDARD	30.000	A1 A2 A1 A3 A1 A2	25.000	L2 L1 L2 L1 L2	
Y1	Marca B	Mod B	STANDARD	20.000	A1 A2 A1 A3 A1 A2	15.000	L2 L1 L2 L1 L2	
Y2	Marca B	Mod C	STANDARD	20.000	A1 A2 A1 A3 A1 A2	15.000	L2 L1 L2 L1 L2	
X01	Marca A	Mod D	STANDARD	50.000	A1 A2 A3 A1 A2 A3	50.000	L2 L1 L2 L1 L2	
X02	Marca A	Mod D	STANDARD	50.000	A1 A2 A3 A1 A2 A3	50.000	L2 L1 L2 L1 L2	
X03	Marca A	Mod D	STANDARD	50.000	A1 A2 A3 A1 A2 A3	50.000	L2 L1 L2 L1 L2	
Y11	Marca B	Mod E	STANDARD	25.000	A1 A2 A3 A1 A2 A3	15.000	L2 L1 L2 L1 L2 L1 L2	
Y12	Marca B	Mod E	STANDARD	25.000	A1 A2 A3 A1 A2 A3	15.000	L2 L1 L2 L1 L2 L1 L2	

Fig. 6. Intervals and systematic preventive maintenance schedule

In the next section will be analyze the method of Uniform Annual Rent (RAU) for determining the economic cycle of buses replacement, we are analyzing a company in the sector of urban transport. Table 7 presents the values related to Linear Depreciation Method, Table 8 the method of Sum of Digits, and Table 9 the Exponential Method.

MP	PROTA	MARCA	MODELO	TPO	1	2	3	4	5	6	7	8	9	10	11	12
X1	Marca A	Mod A	STANDARD	64.350	60.330	57.723	55.942	56.345	49.740	43.303	43.925	52.995				
X2	Marca A	Mod A	STANDARD	65.115	56.358	56.834	51.397	49.177	46.204	51.157	51.717	51.285				
X3	Marca A	Mod A	STANDARD	59.443	61.238	54.267	48.957	57.007	44.875	48.723	53.096	49.445				
Y1	Marca B	Mod B	STANDARD	76.259	66.421	62.647	62.666	66.841	60.873	59.402	68.865	71.815				
Y2	Marca B	Mod C	STANDARD	53.133	62.303	57.642	54.533	59.587	54.370	53.635	58.966	62.455				
X01	Marca C	Mod C	STANDARD	51.644	54.267	51.732	53.327	57.290	59.664	51.308	56.715	51.502				
X02	Marca A	Mod C	STANDARD	53.276	52.633	50.789	51.587	55.364	59.941	54.007	58.395	47.335				
X03	Marca C	Mod D	STANDARD	55.174	61.196	65.235	67.506	69.173	65.586	63.213	59.034	59.707				
Y11	Marca B	Mod E	STANDARD	45.241	62.290	59.294	45.639	43.728	39.754	37.387	36.907	33.382				
Y12	Marca B	Mod E	STANDARD	41.407	60.632	58.460	42.029	41.095	35.199	36.405	32.364	35.807				

Fig. 7. Linear depreciation method Styling

MP	PROTA	MARCA	MODELO	TPO	1	2	3	4	5	6	7	8	9	10	11	12
X1	Marca A	Mod A	STANDARD	64.350	60.330	57.723	55.942	56.345	49.740	43.303	43.925	52.995				
X2	Marca A	Mod A	STANDARD	65.115	56.358	56.834	51.397	49.177	46.204	51.157	51.717	51.285				
X3	Marca A	Mod A	STANDARD	59.443	61.238	54.267	48.957	57.007	44.875	48.723	53.096	49.445				
Y1	Marca B	Mod B	STANDARD	76.259	66.421	62.647	62.666	66.841	60.873	59.402	68.865	71.815				
Y2	Marca B	Mod C	STANDARD	53.133	62.303	57.642	54.533	59.587	54.370	53.635	58.966	62.455				
X01	Marca C	Mod C	STANDARD	51.644	54.267	51.732	53.327	57.290	59.664	51.308	56.715	51.502				
X02	Marca A	Mod C	STANDARD	53.276	52.633	50.789	51.587	55.364	59.941	54.007	58.395	47.335				
X03	Marca C	Mod D	STANDARD	55.174	61.196	65.235	67.506	69.173	65.586	63.213	59.034	59.707				
Y11	Marca B	Mod E	STANDARD	45.241	62.290	59.294	45.639	43.728	39.754	37.387	36.907	33.382				
Y12	Marca B	Mod E	STANDARD	41.407	60.632	58.460	42.029	41.095	35.199	36.405	32.364	35.807				

Fig. 8. Method of Sum of Digits

MP	PROTA	MARCA	MODELO	TPO	1	2	3	4	5	6	7	8	9	10	11	12
X1	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X2	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X3	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X4	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X5	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X6	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X7	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X8	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X9	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X10	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X11	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X12	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X13	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X14	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X15	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X16	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X17	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X18	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X19	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X20	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X21	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X22	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X23	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X24	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X25	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X26	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X27	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X28	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X29	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X30	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X31	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X32	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X33	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X34	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X35	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X36	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X37	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X38	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X39	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X40	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X41	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X42	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X43	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X44	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X45	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X46	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X47	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X48	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X49	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X50	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X51	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X52	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X53	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X54	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X55	10.658.31	8.000.00	0.54	84.801.61	3.388.51	6.799.85	6.990.68	6.990.68	4.337.16	44.027.25	37.78.16	32.381.76	27.730.95	23.616.68	20.483.13	17.614.96
X56	10.

Fig. 12. Gráfico RAU – Bus X2

Fig. 13. Gráfico RAU – Bus X3

Through the analysis of previous data can be seen that the values of rents vehicles are very similar. On Table 10 and the Depreciation Method Exponential it appears that the Uniform Annual Cost is minimal between the twelfth and the sixteenth year (economic life), with an approximate value of € 25,000 / year.

The minor RAU calculated value indicates the respective period (multi-year) in which the equipment must be replaced. This value is equivalent to a minimum income that the equipment would cost annually. It can be concluded that this period corresponds to the ideal time to proceed to the replacement of buses based on the Exponential Method for depreciation. If the methods of depreciation are used and the Linear Sum of Digits it appears that the RAU values decreasing; however there is an increase in the period where the value of RAU is minimal, that is between the sixth and the sixteenth, that create problems to the decision of the ideal moment to replace the equipment.

We can then verify the calculation of Uniform Annual Rent for homogeneous group: B Brand, Model B and C, consisting of two cars of 16 and 14 years (Table 14 and 15).

Valuário Y1									
Ano	Idade	CA (€)	CM (€)	CM (%)	CM (%)	CM (%)	CM (%)	CM (%)	CM (%)
1999	1	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2000	2	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2001	3	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2002	4	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2003	5	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2004	6	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2005	7	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2006	8	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2007	9	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2008	10	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2009	11	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2010	12	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2011	13	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2012	14	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2013	15	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2014	16	24	40	2,00	2,00	2,00	2,00	2,00	2,00

Fig. 14. Tablet RAU – Bus Y1

Valuário Y2									
Ano	Idade	CA (€)	CM (€)	CM (%)	CM (%)	CM (%)	CM (%)	CM (%)	CM (%)
1999	1	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2000	2	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2001	3	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2002	4	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2003	5	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2004	6	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2005	7	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2006	8	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2007	9	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2008	10	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2009	11	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2010	12	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2011	13	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2012	14	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2013	15	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2014	16	24	40	2,00	2,00	2,00	2,00	2,00	2,00

Fig. 15. Tablet RAU – Bus Y2

Fig. 16. Gráfico RAU – Bus Y1

Fig. 17. Gráfico RAU – Bus Y2

Through the analysis of charts of RAU of the buses Y1 and Y2 can be seen that the values of rents vehicles are not identical.

In relation to vehicle Y2 is verified that the RAU will be minimal between the fourth and eleventh years (economic life), with an approximate value of € 35,000 / year.

If the methods of depreciation and Linear Sum of Digits are used can be seen that the RAU values decrease, but occurs an increase of one year in the period where the value of RAU is minimal, which produce problems in the taking of decision of the best time to proceed to the replacement of the equipment.

The Table 18 illustrates the calculation of the RAU to the bus XX1 of the homogeneous group: Brand A, Model B, composed of three vehicles of 10 years; Figures 19 to 20 illustrate the evolution of RAU for XX1, XX2 and XX3.

Valuário XX1									
Ano	Idade	CA (€)	CM (€)	CM (%)	CM (%)	CM (%)	CM (%)	CM (%)	CM (%)
2000	1	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2001	2	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2002	3	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2003	4	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2004	5	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2005	6	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2006	7	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2007	8	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2008	9	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2009	10	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2010	11	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2011	12	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2012	13	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2013	14	24	40	2,00	2,00	2,00	2,00	2,00	2,00
2014	15	24	40	2,00	2,00	2,00	2,00	2,00	2,00

Fig. 18. Tablet RAU – Bus XX1

Fig. 19. Grafic RAU – Bus XX1

Fig. 20. Grafic RAU – Bus XX2

Fig. 21. Grafic RAU – Bus XX3

By the data showed it appears that the replacement period varies from homogenous group to homogeneous group of vehicles and there are several variables that can influence the outcome and the final decision of the manager, such as the apparent rate of each year as well as the depreciation model used. Another very important variable that can significantly influence the results is the maintenance cost. This, in turn, depends heavily on the policies and management of maintenance that is performed at public transport companies.

IV. CONTRIBUTIONS TO THE FLEET RESERVE

The urban transport companies always have a given rate of buses reservation, which varies from company to company. A low reserve ratio is a synonym of high reliability, relying essentially on implementation of an efficient planned maintenance, which results in the application of new methods and maintenance techniques that lead to the assessment of the state of the equipment and the decision of replacing or renewing the equipment's.

There is a common set of factors that affect the optimal size of the number of vehicles in a reserve fleet, that are:

- Composition of the bus fleet;
- Brands and models;
- Age of the fleet;
- Annual rolling of the buses;
- Commercial speed that buses are subject;
- Surrounding and the operating environment;
- Daily fluctuations in the demand for transport;
- Policies and maintenance plans;
- Ratio of vehicles per mechanic;
- Planes maintenance training;
- Number of interventions picket;
- Tunings introduced the routes;
- Tunings introduced in services;
- Inventory management;
- Administration and Finance

To assess the management practices in transport companies the FTA (Federal Transit Administration - USA) conducted a survey of the 36 North American and Canadian companies, which included eight small companies with fleets of between 33 and 199 buses eight medium enterprises with fleets between 225 and 472 bus, 12 large companies with fleets ranging between 537 and 963 buses and eight very large companies with fleets between 1009 and 3664 buses. A synthesis of indicators of activity distributed by classes can be analyzed in Table 22.

Classe empresa	Número de empresas	Taxa de viagens de reserva (%)	Velocidade média (km/h)	Média de Km percorridos por veículo	Idade média da frota (anos)
Pequena	8	19	26,0	54768	7,7
Média	8	20	26,8	59991	8,1
Grande	12	21	26,9	65029	8
Muito grande	8	17	19,3	62771	9,3
Todas	36	20	26,3	61541	8,3

Fig. 22. Indicators of operating fleets, according to their size

The measurement and monitoring of reserve rates continue to be an important management tool in the urban transport sector. The inquire results highlight that transport managers are aware of their responsibility in the management of fleets within reasonable constraints of rolling materials reserve.

Survey responses indicate that efforts are being made in the sector to find ways to reduce the number of units vehicles spares. Many maintenance managers not only follow the guidelines of the FTA regarding the target of 20% of vehicle spares, as they have adopted the philosophy of "the smaller the better" in the managing of their fleets.

Ten percent of the buses are in daily standard repairs. On average, each bus of external service uses the pickets intervention nine times a year. The combined effects of the restrictive legislation of pollution in California, the dedicated maintenance, the high demand of transports and a skewed distribution on age and type of the impact of bus effects have led to an increased rate of reserve vehicles.

As a corollary, it may be noted that the definitions of the indicators of management of urban passenger transport shift

from company to company. It also appears that the technologies used, the accuracy and frequency of collection of values of operating variables and indicators of buses network, the methodology and handle of the data vary significantly from operator to operator.

In urban transport companies there is a great diversity of reserve rates of vehicles, which seems to show empiricism in its determination. It is therefore important to study this discrepancy in terms of optimizing an integrated model of replacement that necessarily implies a rationalization in the reserve fleet. Intends to implemented mathematical modeling of final decision support for replacement of buses of a fleet indexed to the reserve buses fleet. This model will be validated in all its extension in an enterprise of collective transports not only with the aim of the validation, but also to incorporate the goods of the contributions of the managers who will use it.

V. CONCLUSIONS

This article presents a new approach to the economic models to the determination of the most adequate time for a replacement of buses in a urban fleet of an enterprise. The economic aspects were defined in concordance with the pertinent indicators and the cash flow, driven by the cost associated to the acquisitions, maintenance, and operation, among others.

The study presented allows the equipment's life cycle assessment by the managers and obviously it is a decision support tool.

It was demonstrated in the study that exist a variation of ideal moment for as replacement of a vehicle of a fleet, given by the analyses performed by the model of the annual uniform lease. Despite this still to be an anchor point and a useful tool to be used in future models that support the better take of decision. This new models should take in account not only the economics criteria but also non-economics as strategic and management assessed by the multy-dicision tools.

The new model should allow a detailed assessment of the present buses performance against the potential substitutes that turn viable a constant motorization of the goods of the enterprise and keeping high levels of quality and satisfaction of the customer service.

VI. REFERENCES

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